

Practice**Properties of Logarithms**

Use $\log_{10} 5 \approx 0.6990$ and $\log_{10} 7 \approx 0.8451$ to approximate the value of each expression.

1. $\log_{10} 35$ _____ 2. $\log_{10} 25$ _____ 3. $\log_{10} \frac{7}{5}$ _____ 4. $\log_{10} \frac{5}{7}$ _____
 5. $\log_{10} 245$ _____ 6. $\log_{10} 175$ _____ 7. $\log_{10} 0.2$ _____ 8. $\log_{10} \frac{25}{7}$ _____

Solve each equation. Check your solutions.

9. $\log_7 n = \frac{2}{3} \log_7 8$ _____ 10. $\log_{10} u = \frac{3}{2} \log_{10} 4$ _____
 11. $\log_6 x + \log_6 9 = \log_6 54$ _____ 12. $\log_8 48 - \log_8 w = \log_8 4$ _____
 13. $\log_9 (3u + 14) - \log_9 5 = \log_9 2u$ _____ 14. $4 \log_2 x + \log_2 5 = \log_2 405$ _____
 15. $\log_3 y = -\log_3 16 + \frac{1}{3} \log_3 64$ _____ 16. $\log_2 d = 5 \log_2 2 - \log_2 8$ _____
 17. $\log_{10} (3m - 5) + \log_{10} m = \log_{10} 2$ _____ 18. $\log_{10} (b + 3) + \log_{10} b = \log_{10} 4$ _____
 19. $\log_8 (t + 10) - \log_8 (t - 1) = \log_8 12$ _____ 20. $\log_3 (a + 3) + \log_3 (a + 2) = \log_3 6$ _____
 21. $\log_{10} (r + 4) - \log_{10} r = \log_{10} (r + 1)$ _____ 22. $\log_4 (x^2 - 4) - \log_4 (x + 2) = \log_4 1$ _____
 23. $\log_{10} 4 + \log_{10} w = 2$ _____ 24. $\log_8 (n - 3) + \log_8 (n + 4) = 1$ _____
 25. $3 \log_5 (x^2 + 9) - 6 = 0$ _____ 26. $\log_{16} (9x + 5) - \log_{16} (x^2 - 1) = \frac{1}{2}$ _____
 27. $\log_6 (2x - 5) + 1 = \log_6 (7x + 10)$ _____ 28. $\log_2 (5y + 2) - 1 = \log_2 (1 - 2y)$ _____
 29. $\log_{10} (c^2 - 1) - 2 = \log_{10} (c + 1)$ _____ 30. $\log_7 x + 2 \log_7 x - \log_7 3 = \log_7 72$ _____
 31. **SOUND** Recall that the loudness L of a sound in decibels is given by $L = 10 \log_{10} R$, where R is the sound's relative intensity. If the intensity of a certain sound is tripled, by how many decibels does the sound increase?

 32. **EARTHQUAKES** An earthquake rated at 3.5 on the Richter scale is felt by many people, and an earthquake rated at 4.5 may cause local damage. The Richter scale magnitude reading m is given by $m = \log_{10} x$, where x represents the amplitude of the seismic wave causing ground motion. How many times greater is the amplitude of an earthquake that measures 4.5 on the Richter scale than one that measures 3.5?
